



Innovations and networking
in European Forestry

18-19 April 2024
VALLADOLID

ONEforest
Final Conference  ONEforest

The Multicriteria Decision Support System (MCDSS)

Prof. Dr. Udo Buscher, TU Dresden





Outline

- MCDSS – Recap
- Mathematical Model
- Example - Case Study Region Catalonia
- Results



MCDSS - Recap

Goals and characteristics:

- Develop a decision support system for stakeholders
- Find optimal assignment of management option to cells
- Planning horizon: 40 years (2020 – 2060)
- Consideration of user preferences / requirements
- Incorporate simulation data from representative stands of four case study regions (Estonia, Switzerland, Spain, Germany)

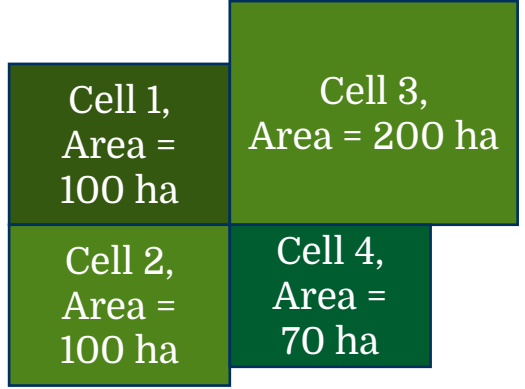


MCDSS - Recap

Initial stand	Species 1	Species 2
	share	share	share	
1	10	10
2	10	10
3	50	50
...
	0	100

Initial Stand	Management option	Indicators ≈ 20				
		0	1	2	...	8
1	A	0	1	1	...	5
1	B	1	0	1	...	0
1	C	1	1	1	...	1
1	D	1	2	0	...	0
2	A
2	B
2	C
2	D
...	
	A
	B
	C
	D

recreate own forest with representative stands



Cell	Management option
1	A
2	B
3	A
4	D

Management options:

- A: low intensity
- B: business as usual
- C: climate adapted forestry
- D: intensified management

assign one management option to each of the cells



MCDSS - Recap

Indicator List

- Standing timber
- Harvested timber (total + assortments)
- Periodic annual increment
- Quadratic mean diameter
- Height variability (mean + SD)
- Diameter variability (mean + SD)
- Deadwood
- Shannon index
- Carbon in stock
- Carbon sequestration
- Number of large trees
- Visual attractiveness
- Wood revenues
- Risk of total loss
- Risk of economic loss



Mathematical Model



Mathematical Model

Mixed Integer (Linear) Program



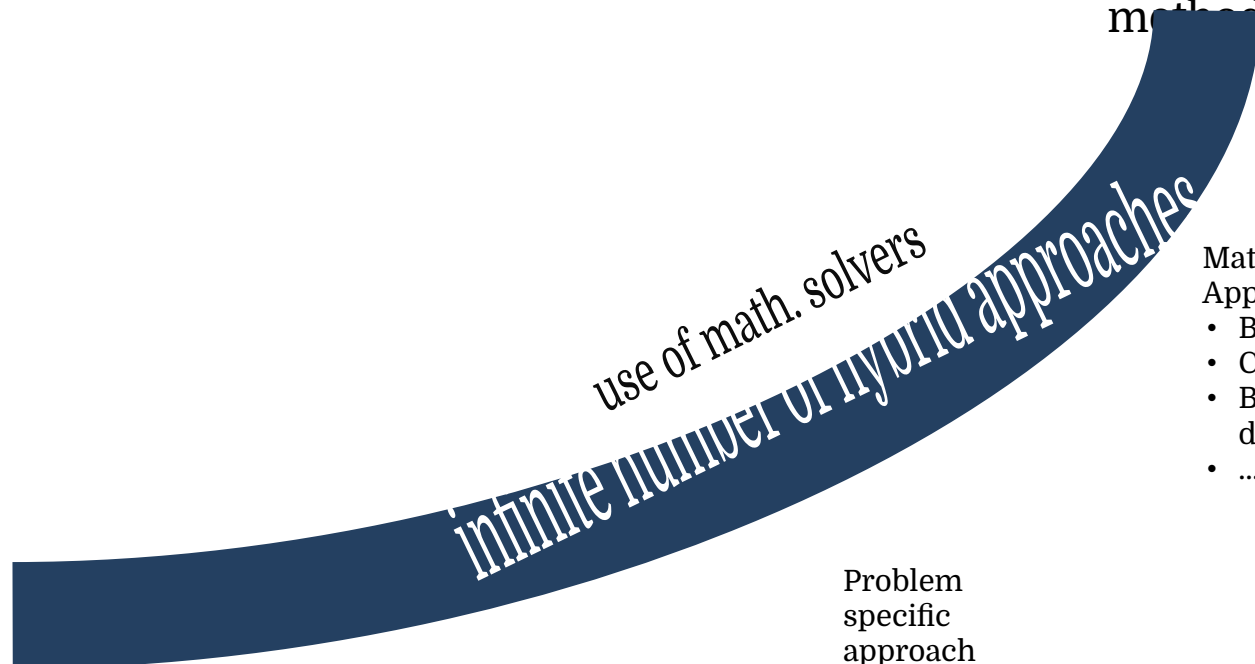
Exact solution methods

$$\max c^T x$$

$$\text{subject to: } A \cdot x \leq B, \\ x \in \mathbb{Z}^+$$



Heuristic solution methods



use of math. solvers

infinite number of hybrid approaches

Problem specific approach

- Meta-Heuristics
- Genetic algorithm
 - Tabu-Search
 - Simulated Annealing
 - ...

- Mathematical Approaches
- Branch & Bound
 - Column Generation
 - Benders decomposition
 - ...



Mathematical Model

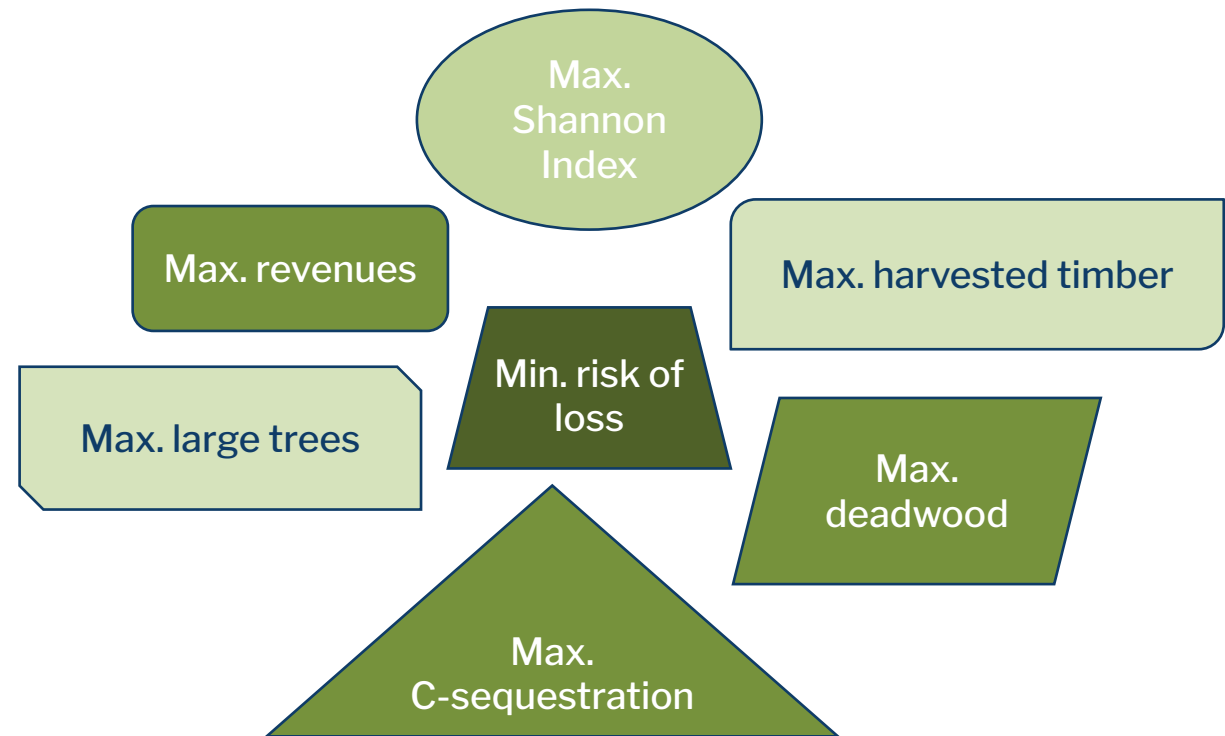
Weighted Sum Approach

$$T \cdot x + \beta \cdot c_1^T \cdot x$$

...

s.t. $A \cdot x \leq B,$

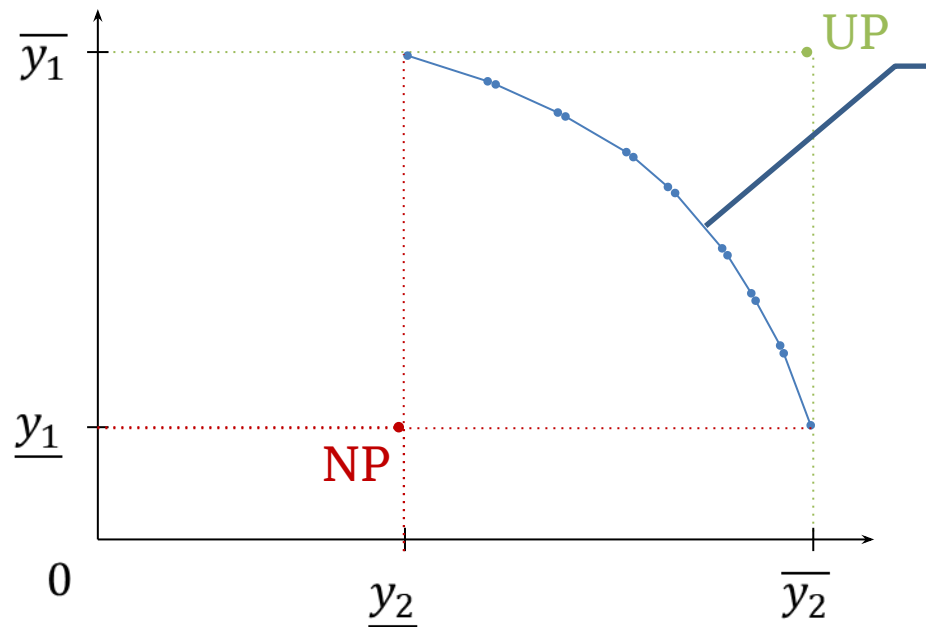
$$x \geq 0.$$





Mathematical Model

Weighted Sum Approach



Pareto optimality: There is no solution that has a higher value of y_2 without a deterioration of y_1 .

decision maker



Without preferences:

- is indifferent between all solutions that are on the pareto frontier



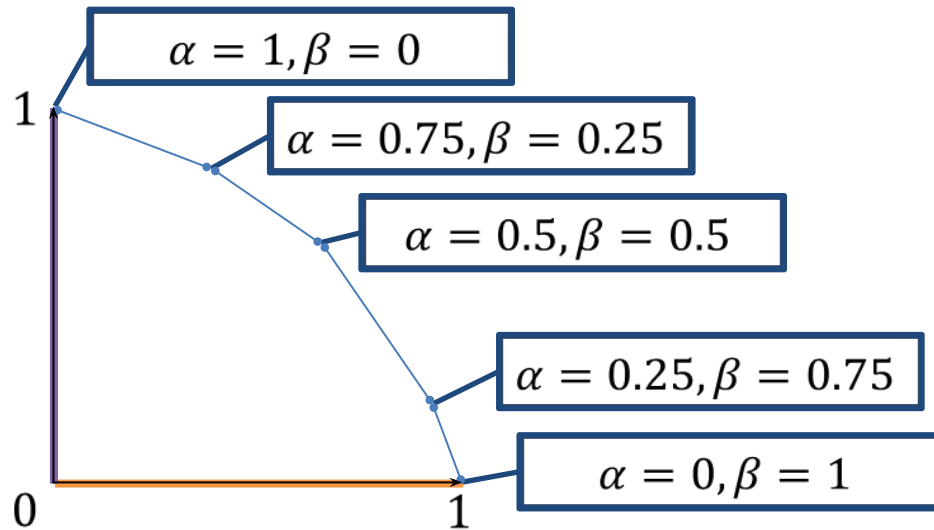
With preferences:

- finds its best solution on the pareto frontier



Mathematical Model

Weighted Sum Approach

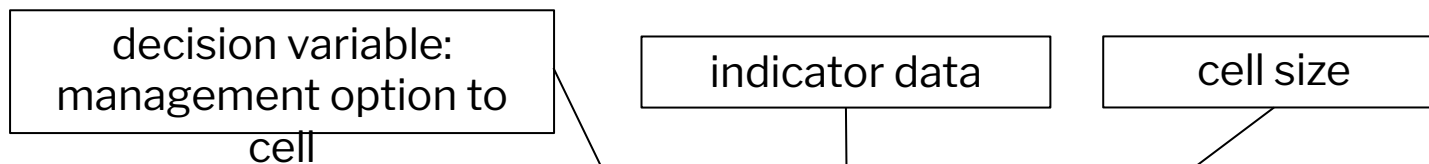


$$\max \alpha \cdot y_1^* + \beta \cdot y_2^*$$
$$\alpha + \beta = 1$$



Mathematical Model

Indicators



Harvested timber

$$v_{(\text{harvested timber}),g} = \sum_{t \in T} \sum_{c \in C_g} \sum_{m \in M} x_{c,m} \cdot B_{c,m,t}^{\text{HarvestedTimber}} \quad \forall g \in G$$

Carbon-sequestration

$$v_{(c\text{-sequestration}),g} = \sum_{t \in T} \sum_{c \in C_g} \sum_{m \in M} x_{c,m} \cdot B_{c,m,t}^{\text{Carbon}} \cdot l \quad \forall g \in G$$

Standing timber

$$v_{(\text{standing timber}),g} = \sum_{t \in T} \sum_{c \in C_g} \sum_{m \in M} x_{c,m} \cdot B_{c,m,t}^{\text{Standing}} \quad \forall g \in G$$

Large trees

$$v_{(\text{large trees}),g} = \sum_{t \in T} \sum_{c \in C_g} \sum_{m \in M} x_{c,m} \cdot B_{c,m,t}^{\text{Trees}} \cdot F_c \quad \forall g \in G$$

...

...

...



Shannon Index

Mathematical Model

$$v_{(shannon\ index),g} = - \sum_{t \in T} \sum_{c \in C_g} \sum_{m \in M} \sum_{s \in S} x_{c,m} \cdot F_{c,m,s,t} \cdot \ln(x_{c,m} \cdot F_{c,m,s,t}) \quad \forall g \in G$$

not linear!

=> Approximation through linearization necessary!

Assumption: Shannon index reaches the maximum if following statement applies:

$$\sum_{c \in C_g} \sum_{m \in M} x_{c,m} \cdot F_{c,m,s,t} = \frac{1}{|S|} \quad \forall t \in T, s \in S$$

The area share of all species should be as equal as possible



$$\min \hat{y} = \sum_{t \in T} \sum_{s \in S} (u_{t,s} + o_{t,s})$$

The deviation to the theoretical optimal share is minimized

s.t.:

$$\sum_{c \in C_g} \sum_{m \in M} x_{c,m} \cdot F_{c,m,s,t} + u_{t,s} - o_{t,s} = \frac{1}{|S|}$$

$\forall s \in S, t \in T$

$$u_{t,s} \leq s_{t,s} \quad \forall s \in S, t \in T$$

$$o_{t,s} \leq 1 - s_{t,s} \quad \forall s \in S, t \in T$$

$$0 \leq o_{t,s}, u_{t,s} \leq 1 \quad \forall s \in S, t \in T$$

$$s_{t,s} \in \{0; 1\} \quad \forall s \in S, t \in T$$



Mathematical Model

Selecting one management option for each cell

Maximize weighted sum
objective:

User constraints and goal
programming possible, e.g.

$$\sum_{c \in C_g} \sum_{m \in M} x_{c,m} \cdot B_{c,m,t}^{Trees} \begin{matrix} \leq \\ \geq \end{matrix} Limit \quad \forall t \in T$$

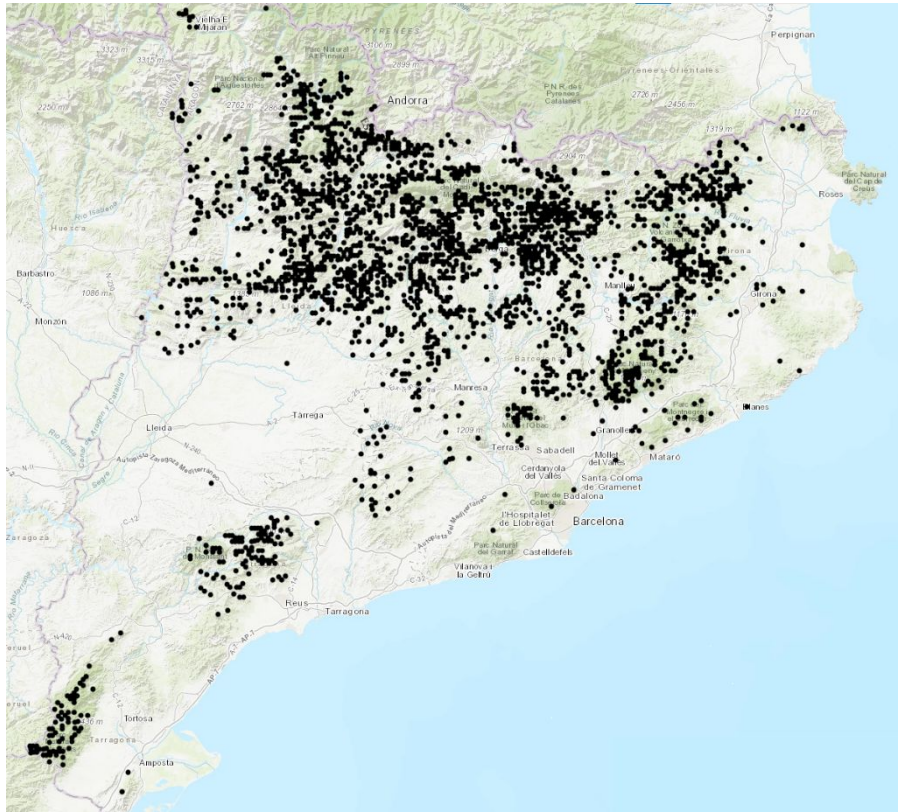
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Example - Case Study Region Catalonia



CSR Catalonia - Example



- 18 representative stands
 - Species code (Pinus sylvestris, Pinus nigra, Quercus ilex)
 - Site-quality index (high, low)
 - Stand age (young, based, mature)
- Simulation data for 19 indicators (each for the 18 stands and the planning horizon of 2020 - 2060)
- 2693 cells
- 4 management options
 - A: Low intensity management / biodiversity
 - B: Protection function / Business as usual (BAU)
 - C: Climate-adapted forestry
 - D: Wood production



CSR Catalonia - Example

18
stands

ONEForest
Project About 0.1.1

Cells Policies Objectives Constraints Optimization

Select Region: WP3_MediterraneanForests_Spain Periods: 8 Read data

stand	species1	species2	species3	species4	species5	species6	species7	species8	species9	species10
21_HIGH_MEDI...	Crataegus spp	Pinus sylvestris	Crataegus mon...	Pinus uncinata	Pinus pinea	Pinus halepensis	Quercus humilis	Pinus nigra	Fraxinus excelsi...	Ulmus glab
21_HIGH_YOUNG	Pinus sylvestris	Crataegus mon...	Pinus uncinata	Quercus humilis	Pinus nigra	Juniperus com...	Quercus petraea	Quercus faginea	Quercus ilex	Acer opalu:
21_HIGH_MATU...	Pyrus spp	Pinus sylvestris	Crataegus mon...	Pinus uncinata	Pinus pinea	Quercus humilis	Pinus nigra	Pinus pinaster	Betula alba	Abies alba
25_HIGH_MEDI...	Crataegus spp	Pinus sylvestris	Crataegus mon...	Pinus pinea	Pinus halepensis	Quercus humilis	Pinus nigra	Pinus pinaster	Juniperus com...	Juniperus p
25_HIGH_YOUNG	Pinus sylvestris	Pinus pinea	Juniperus oxyc...	Pinus halepensis	Quercus humilis	Pinus nigra	Acer monspess...	Juniperus com...	Quercus faginea	Quercus ile
25_HIGH_MATU...	Pinus sylvestris	Pinus halepensis	Quercus humilis	Pinus nigra	Sorbus aucuparia	Quercus ilex	Acer opalus			

Size Name

Add cell Remove cell load CSS / CSR cells Add group Remove group

cell	size	stand
1	162,3113757	21_LOW_YOUNG
2	143,1009052	21_LOW_MATURE
3	143,1009052	21_HIGH_MEDIUM
4	143,1009052	21_HIGH_YOUNG
5	143,1009052	21_HIGH_MEDIUM
6	162,3113757	21_LOW_MEDIUM
7	143,1009052	21_HIGH_MEDIUM
8	143,1009052	21_HIGH_MEDIUM
9	143,1009052	21_LOW_MEDIUM

2693 cells
with
correspondin
g stand and
size



CSR Catalonia - Example

Weights for indicators are predefined for four scenarios (THRO / SLU)

	Scenario I Society under voluntary green transition	Scenario II Climate change adaption and green transition	Scenario III Protection and recreation-oriented forest management	Scenario IV Climate change mitigation in a slow- growing bioeconomy
Standing timber		5	10	10
Harvested timber total	50	30	10	20
Periodic annual increment	5	5	5	5
QMD (harvested species)	5	3		
QMD (harvested stand)	10	3		
QMD (standing species)		2	5	
QMD (standing stand)		2	5	
Height variability (SD)				5
Diameter variability (mean)				5
Deadwood with decomposition			10	10
Carbon in stock aboveground		5		5
Carbon sequestration	5	15		10
Number of large trees		5	20	10
Visual attractiveness		5	20	10
Risk of economic loss		5		
Shannon index	5	5	15	10
Wood revenues	20	10		



CSR Catalonia - Example

Weighted sum objective based on the predefined weights (here: Scenario I)

The screenshot shows the ONEForest software interface. The 'Objectives' tab is active, displaying a list of objectives under the 'Global' category. 'Harvested Timber (total)' is selected. The configuration panel shows the following settings:

- First period: 0
- Last period: 8
- Indicator: Harvested Timber (total)
- Group: Global
- Weight (in group): 50 (indicated by a slider)
- Use target value?

At the bottom, the objective formula is displayed:

$$\text{Objective} = 1 * (0,5 * \text{Harvested Timber (total)} + 0,05 * \text{Periodic Annual Increment} + 0,05 * \text{QMD Harvested Species} + 0,1 * \text{QMD Harvested Stand} + 0,05 * \text{Shannon Index} + 0,2 * \text{Wood Revenues} + 0,05 * \text{Carbon Sequestration} + 0 * \text{Standing Timber} + 0 * \text{QMD Standing Species} + 0 * \text{QMD Standing Stand} + 0 * \text{Height Variability (SD)} + 0 * \text{Diameter Variability (Mean)} + 0 * \text{Deadwood} + 0 * \text{Carbon in Stock (Aboveground)} + 0 * \text{Number of Large Trees} + 0 * \text{Visual Attractiveness} + 0 * \text{Risk of Total Loss RCP 4.5})$$



CSR Catalonia - Example

Solve mathematical model

The screenshot shows the ONEForest software interface. The 'Optimization' tab is active, displaying settings for the solver and method. The 'Method' is set to 'Weighted_Sum' and the 'Solver' is 'Gurobi'. A 'Go!' button is visible. Below the settings, a log window displays the following text:

```
[Start] Create Objective
      Computation Time: 0,0475666
[End] Create Objective
[Start] Optimize Model using objective QMD Standing Species_Global
      Computation Time: 1,9232245
[End] Optimize Model
[Start] Create Objective
      Computation Time: 0,0021714
[End] Create Objective
[Start] Optimize Model using objective QMD Standing Stand_Global
      Computation Time: 2,0451042
[End] Optimize Model
[Start] Create Objective
      Computation Time: 0,0021589
[End] Create Objective
[Start] Optimize Model using objective Height Variability (SD)_Global
      Computation Time: 2,0318279
[End] Optimize Model
[Start] Create Objective
      Computation Time: 0,0023281
[End] Create Objective
[Start] Optimize Model using objective Diameter Variability (Mean)_Global
      Computation Time: 1,8521976
[End] Optimize Model
[Start] Create Objective
      Computation Time: 0,0041477
[End] Create Objective
[Start] Optimize Model using objective Deadwood_Global
```



Results



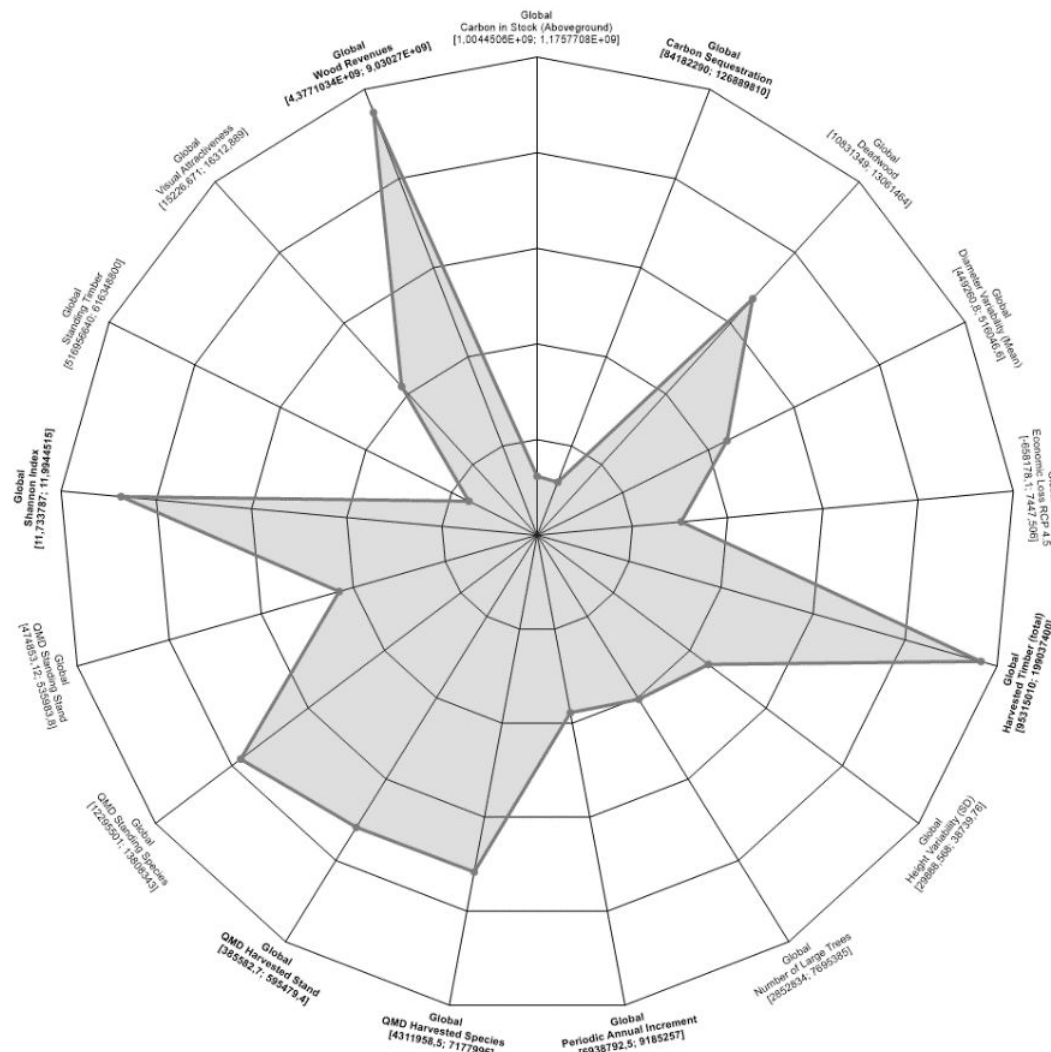
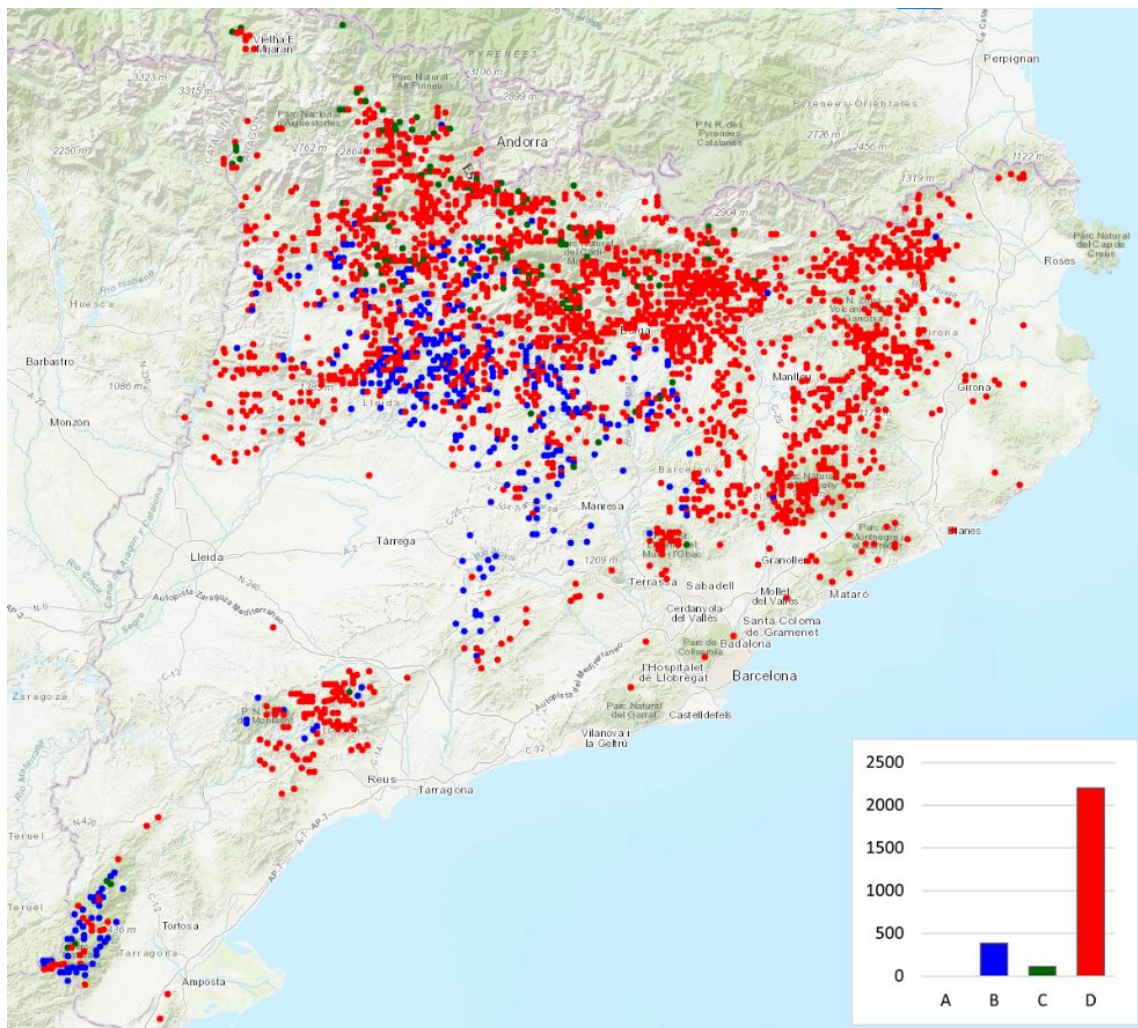
Results

	A	B	C	D	E	F	G	H	I	J	K	L	M
1	Objective	0,8486											
2	Computation Time	66,2785221											
3	MIP Gap	NaN											
4													
5	group	obj	lb	ub	objValue								
6	Global	Harvested Timber (total)	95315007,3	199037400	195423886,4								
7	Global	Periodic Annual Increment	6938792,489	9185256,94	7787285,573								
8	Global	QMD Harvested Species	4311958,507	7177996,16	6366197,087								
9	Global	QMD Harvested Stand	385582,6796	595479,403	536418,7324								
10	Global	Shannon Index	11,73378668	11,9944512	11,96166066								
11	Global	Wood Revenues	4377103291	9030269783	8788521103								
12	Global	Carbon Sequestration	84182291,67	126889810	89259010,78								
13	Global	Standing Timber	516956634,7	616348774	532825785,4								
14	Global	QMD Standing Species	12295500,71	13808342,7	13471288,78								
15	Global	QMD Standing Stand	474853,1271	535983,823	501174,3526								
16	Global	Height Variability (SD)	29888,5675	38739,7614	33859,16661								
17	Global	Diameter Variability (Mean)	449260,8015	516046,606	478892,9411								
18	Global	Deadwood	10831349,04	13061463,9	12323388,7								
19	Global	Carbon in Stock (Aboveground)	1004450633	1175770764	1025566546								
20	Global	Number of Large Trees	2852834,009	7695385,11	4808010,226								
21	Global	Visual Attractiveness	15226,6713	16312,8882	15683,64655								
22	Global	Economic Loss RCP 4.5	-658178,1021	7447,5058	-456730,3702								
23													
24	stand	cell	mgmt opt	id									
25	21_LOW_YOUNG	1	D	80004									
26	21_LOW_MATURE	2	C	80006									
27	21_HIGH_MEDIUM	3	D	80012									
28	21_HIGH_YOUNG	4	D	80014									
29	21_HIGH_MEDIUM	5	D	80015									
30	21_LOW_MEDIUM	6	D	80019									
31	21_HIGH_MEDIUM	7	D	80020									
32	21_HIGH_MEDIUM	8	D	80021									
33	21_LOW_MEDIUM	9	D	80022									
34	21_LOW_MEDIUM	10	D	80024									
35	21_LOW_MEDIUM	11	D	80025									

- Detailed numerical output
- Value for all indicators and value range (lower bound / upper bound)
- Optimal assignment of management options to cells

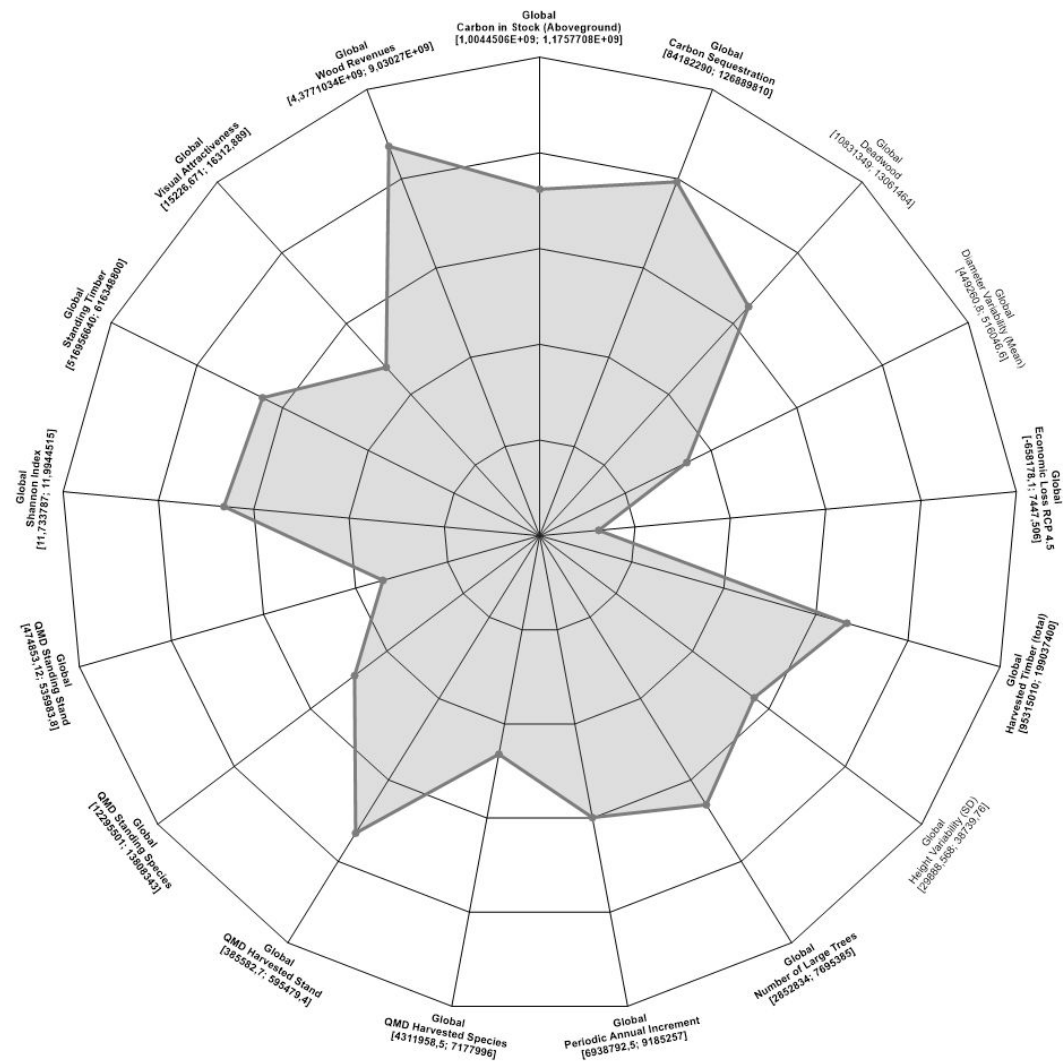
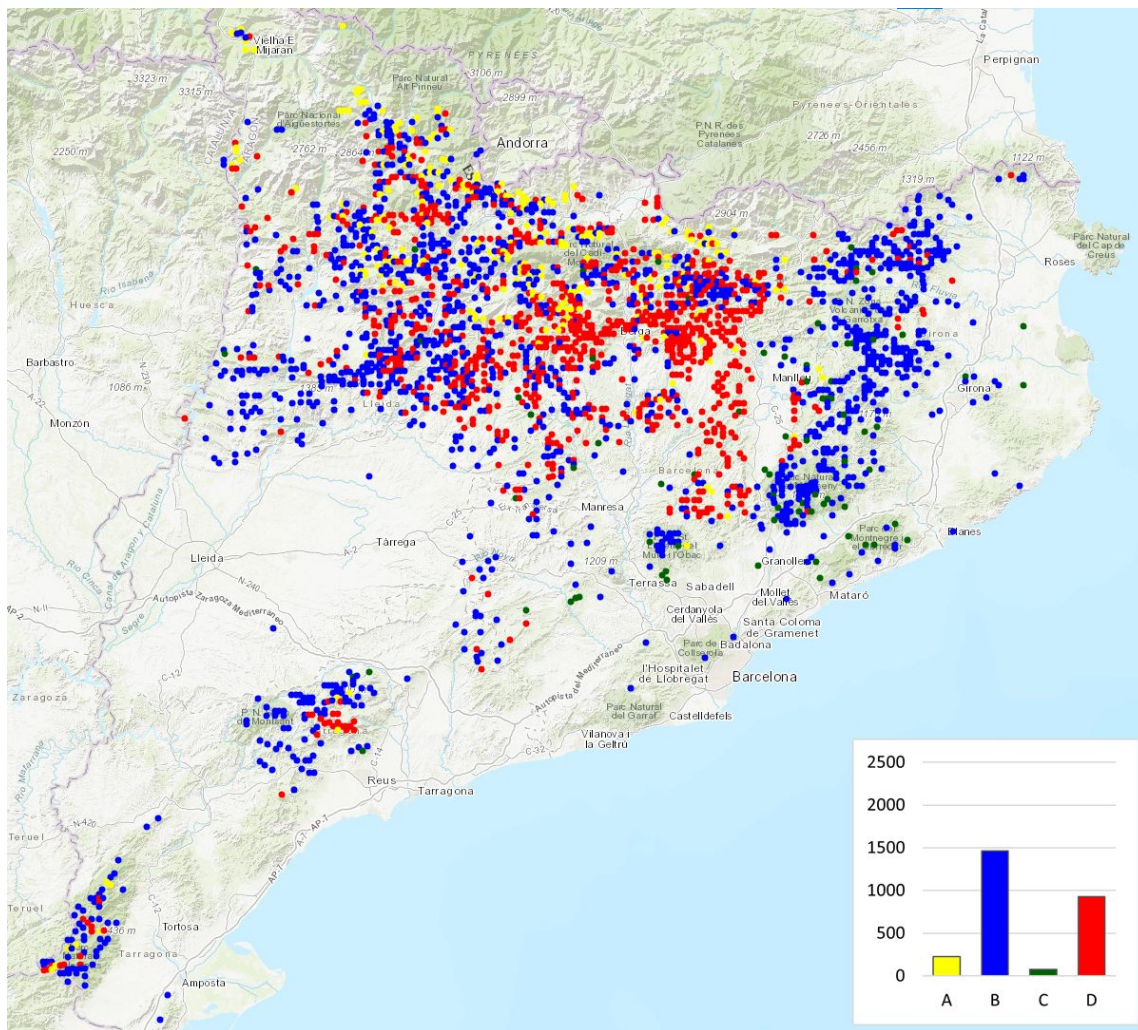


Results - Scenario I



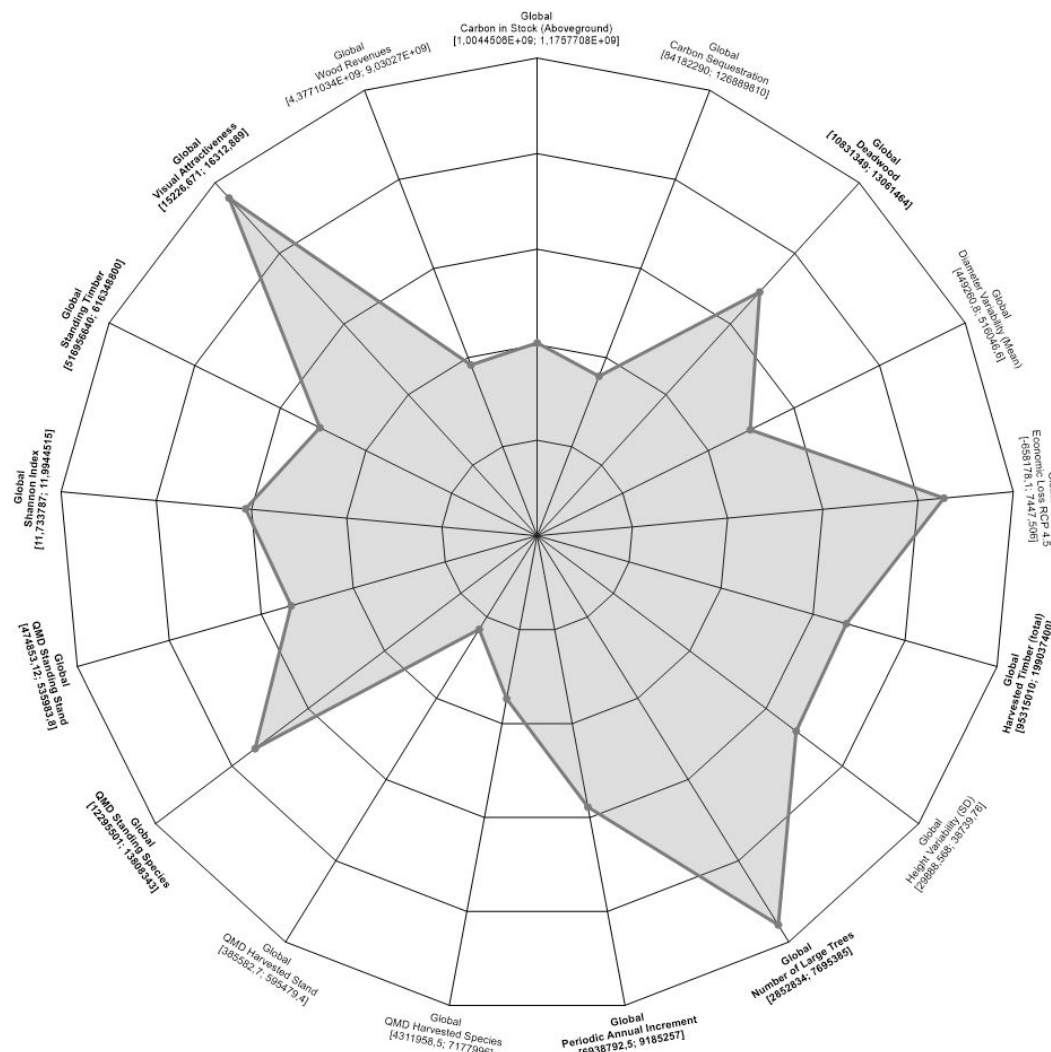
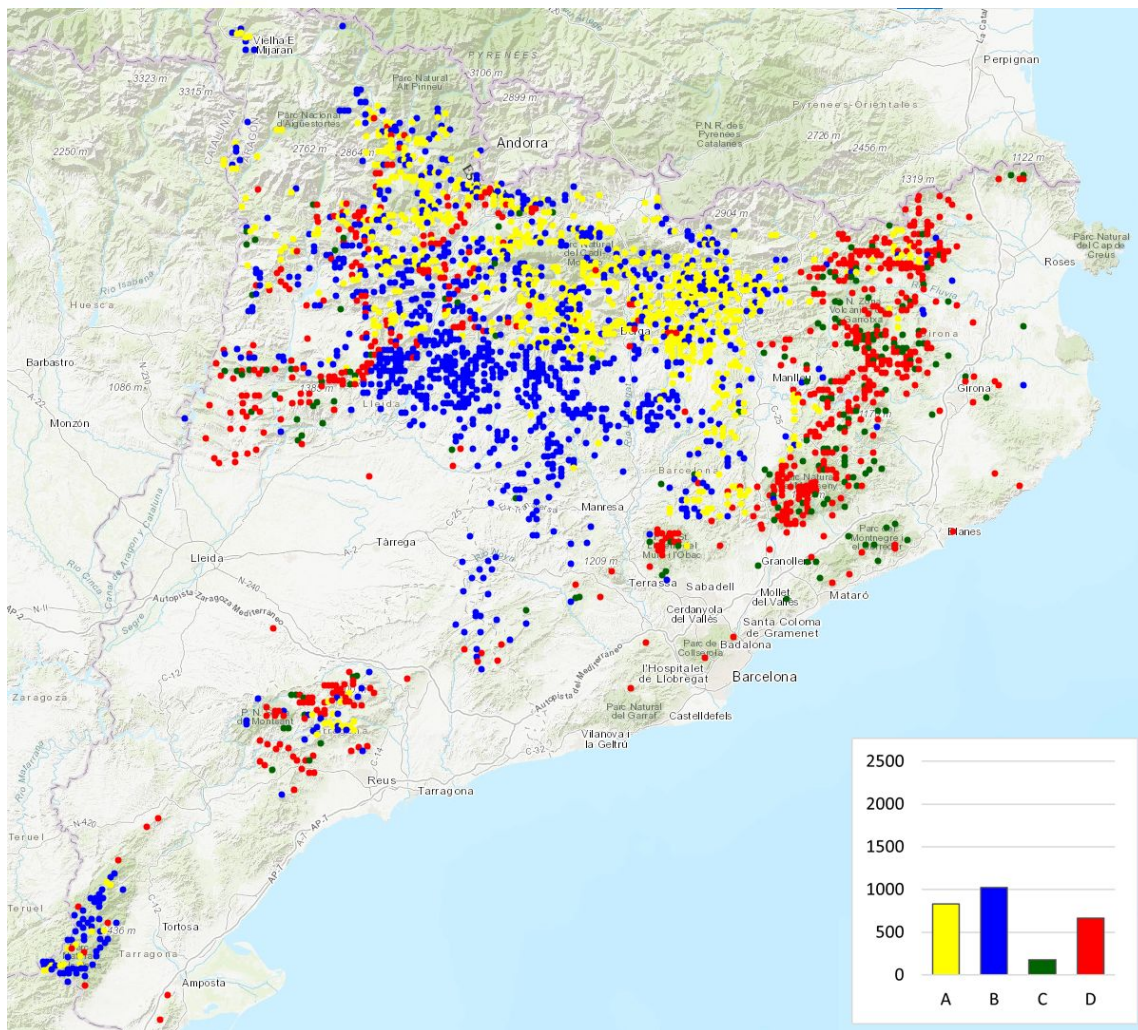


Results - Scenario II



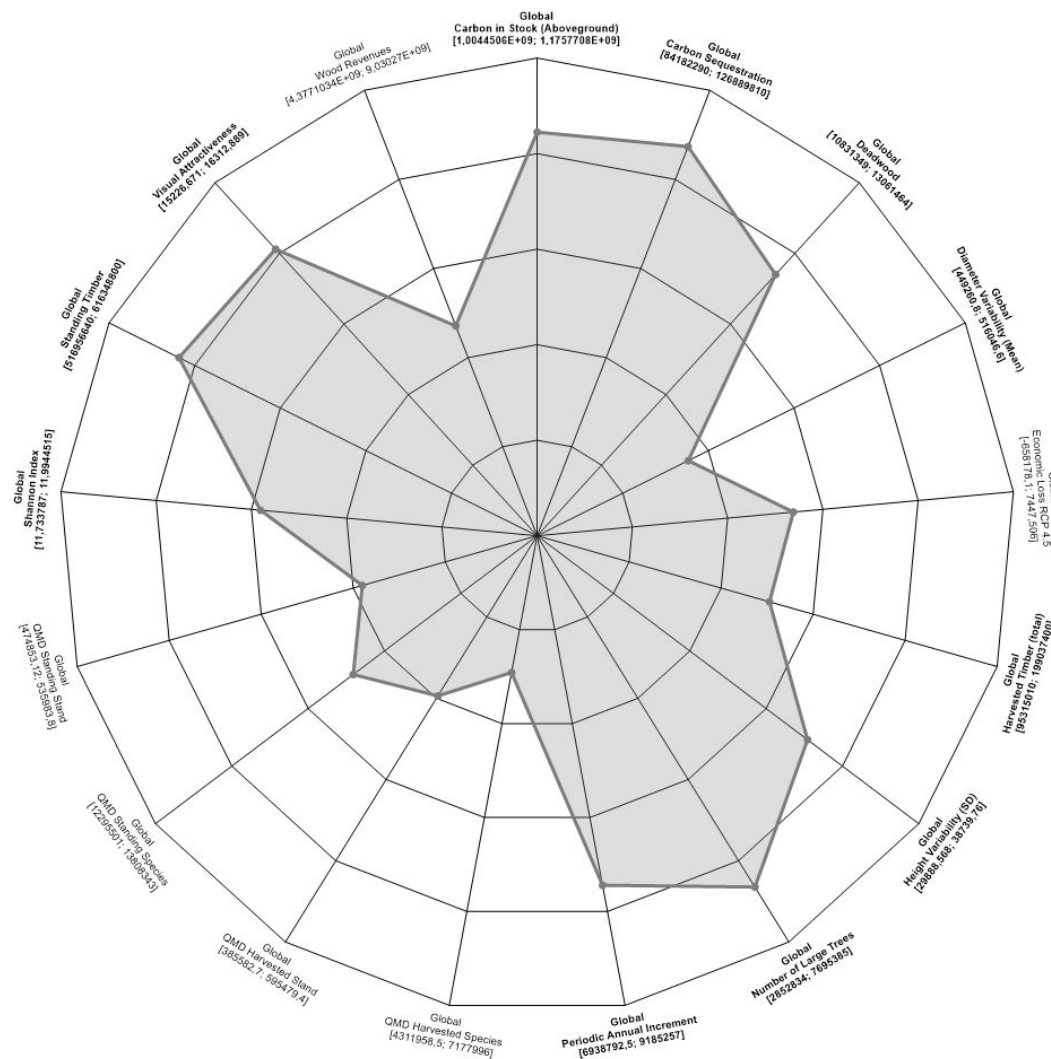
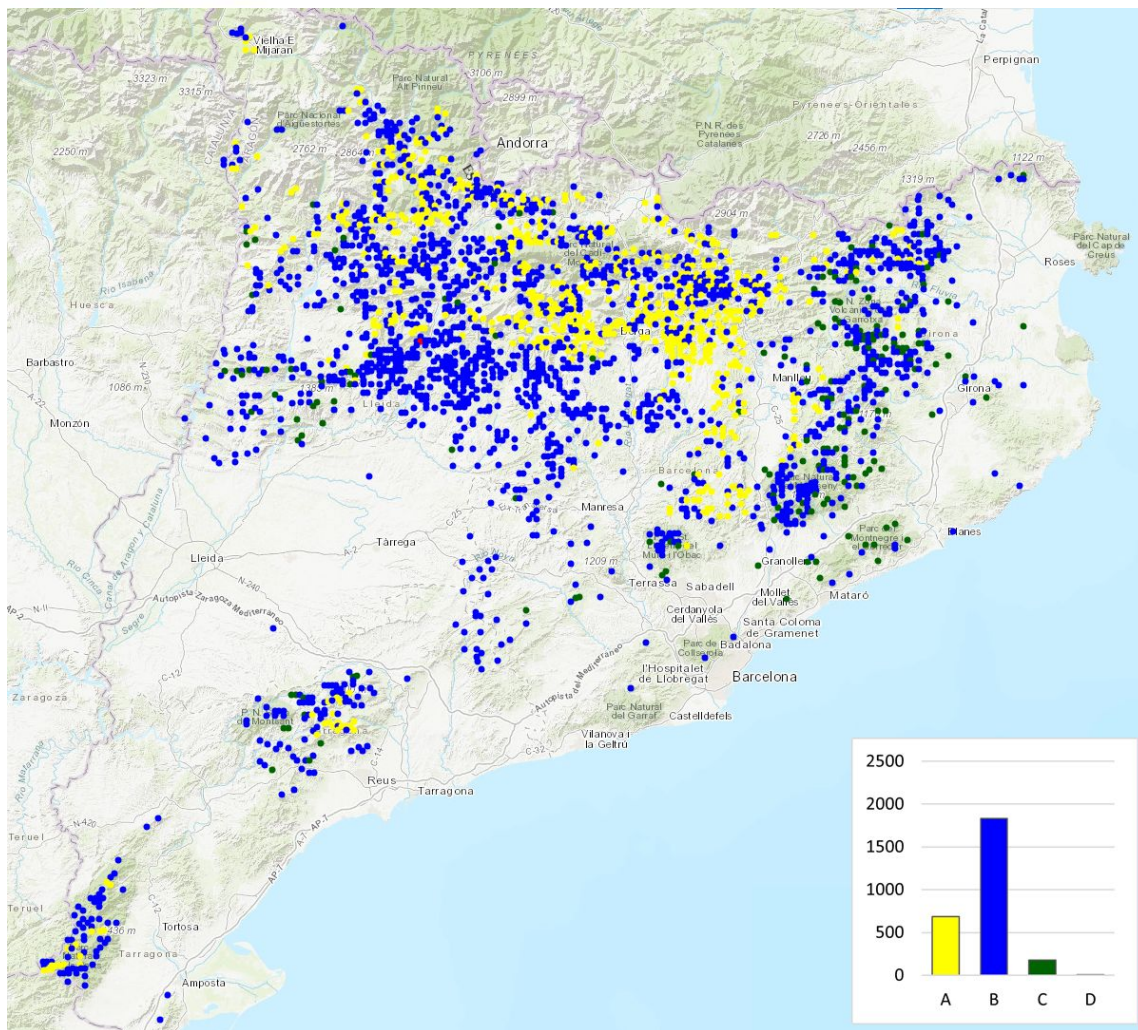


Restuls - Scenario III





Results - Scenario IV





Conclusion

- The MCDSS helps stakeholders make informed, number-based decisions
- The simulation data from the case study regions serve as input for a mathematical model based on the weighted sum approach
- The results should be understood as suggestions for further analyses
- There is not ONE optimal solution because the results depend heavily on the weightings applied



ONEforest



This project has received funding from the European Union's Horizon 2020 research and innovation programme under the grant agreement N° 101000406.

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